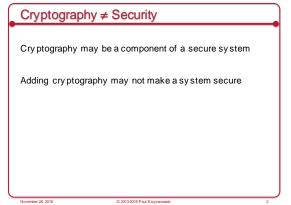
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### Distributed Systems 24. Cry ptographic Systems: An Brief Introduction Paul Krzyzanowski Rutgers University Fall 2016



Cryptography: what is it good for?

- Authentication
- determine origin of message
- verify that message has not been modified
- Nonrepudiation
- sender should not be able to falsely deny that a message was sent
- Confidentiality
- others cannot read contents of the message

**Terms** Plaintext (cleartext) message P Encryption E(P) Produces Ciphertext, C = E(P)Decryption, P = D(C)Cipher = cryptographic algorithm

Terms: types of ciphers

- · Restricted cipher
- · Symmetric algorithm

· Public key algorithm

Restricted cipher

Secret algorithm

- If you know the algorithm, you can encrypt & decrypt
- · Vulnerable to:
- Leaking
- Reverse engineering
- Hard to validate its effectiveness (who will test it?)
- · Not a viable approach!

### Symmetric-key algorithm

- Known algorithm but we introduce a secret parameter the key
- · Same secret key, K, for encryption & decryption

 $C = E_K(P)$  $P = D_K(C)$ 

• Examples: AES, 3DES, IDEA, RC5

· Key length

- Determines number of possible keys
- DES: 56-bit key:  $2^{56} = 7.2 \times 10^{16}$  keys
- AES-256: 256-bit key: 2<sup>256</sup> = 1.1 x 10<sup>77</sup> keys
- Brute force attack: try all keys

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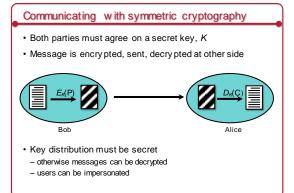
### The power of 2 Adding one extra bit to a key doubles the search space Suppose it takes 1 second to search through all keys with a 20-bit key key length number of keys search time 20 bits 1,048,576 1 second

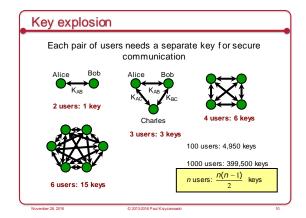
key length	number of keys	search time
20 bits	1,048,576	1 second
21 bits	2,097,152	2 seconds
32 bits	$4.3 \times 10^{9}$	~ 1 hour
56 bits	$7.2 \times 10^{16}$	2,178 years
64 bits	$1.8 \times 10^{19}$	> 557,000 years
256 bits	$1.2 \times 10^{77}$	$3.5 \times 10^{63}$ years

Distributed & custom hardware efforts typically allow us to search between 1 and >100 billion 64-bit (e.g., RC5) keys per second

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## Key distribution Secure key distribution is the biggest problem with symmetric cry ptography

Diffie-Hellman Key Exchange

Key distribution algorithm

- First algorithm to use public/priv ate "key s"

- Not public key encryption

- Uses a one-way function
Based on difficulty of computing discrete logarithms in a finite field compared with ease of calculating exponentiation

Allows us to negotiate a secret common key without fear of eavesdroppers

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### Diffie-Hellman Key Exchange

All arithmetic performed in a field of integers modulo some large number

- Both parties agree on a large prime number p and a number  $\alpha < p$
- · Each party generates a public/private key pair

Private key for user i: Xi

<u>Public</u> key for user i:  $Y_i = \alpha^{X_i} \mod p$ 

### Diffie-Hellman exponential key exchange

- Alice has secret key X<sub>A</sub>
- Bob has secret key X<sub>B</sub>
- Alice has public key Y<sub>A</sub>
- Bob has public key YB
- · Alice computes

$$K = Y_B^{X_A} \mod p$$

K = (Bob's publickey) (Alice's private key) mod p

### Diffie-Hellman exponential key exchange

- Alice has secret key X<sub>A</sub>
- Alice has public key Y<sub>A</sub>
- · Alice computes

$$K = Y_B^{X_A} \mod p$$

- Bob has secret key X<sub>B</sub>
- Bob has public key Y<sub>B</sub>
- · Bob computes

$$K = Y_A^{X_B} \mod p$$

 $K' = (Alice's public key)^{(Bob's private key)} mod p$ 

### Diffie-Hellman exponential key exchange

- Alice has secret key X<sub>A</sub>
- Alice has public key Y<sub>A</sub>
- · Alice computes  $K = Y_B^{X_A} \mod p$
- · expanding:
- $K = Y_B^{X_A} \operatorname{mod} p$
- $= (\alpha^{X_B} \mod p)^{X_A} \mod p$
- $= \alpha^{X_B X_A} \mod p$

· expanding:  $K = Y_B^{X_B} \mod p$ 

· Bob computes

 $= (\alpha^{X_A} \mod p)^{X_B} \mod p$  $= \alpha^{X_A X_B} \mod p$ 

• Bob has secret key XB

• Bob has public key YB

 $K = Y_A^{X_B} \mod p$ 

K = K'

K is a common key, known only to Bob and Alice

### RSA Public Key Cryptography

- · Ron Rivest, Adi Shamir, Leonard Adleman created a public key encryption algorithm in 1977
- · Each user generates two keys:
- Private key (kept secret)
- Public key (can be shared with anyone)
- · Algorithm based on the difficulty of factoring large numbers
- keys are functions of a pair of large (~300 digits) prime numbers

### Public-key algorithm

Two related keys:

$$C = E_{K1}(P)$$
  $P = D_{K2}(C)$   $K_1$  is a public key  $K_2$  is a private key

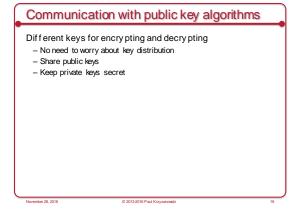
K₁ is a public key

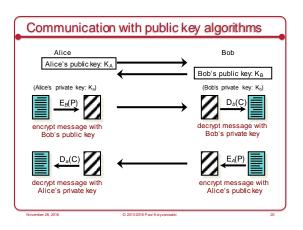
### Examples:

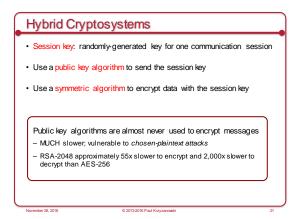
- RSA and Elliptic curve algorithms
- DSS (digital signature standard)

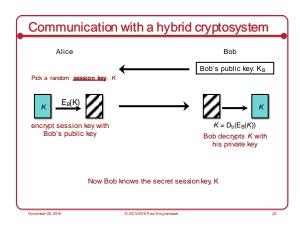
### Key length

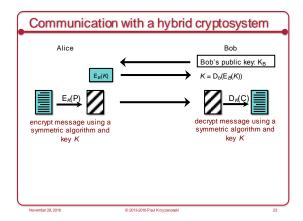
- Unlike symmetric cryptography, not every number is a valid key
- 3072-bit RSA = 256-bit elliptic curve = 128-bit symmetric cipher
- 15360-bit RSA = 521-bit elliptic curve = 256-bit symmetric cipher

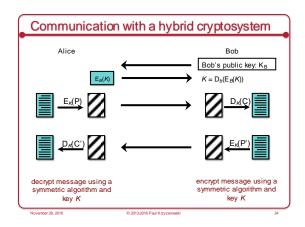












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## Message Authentication

### One-way functions

- Easy to compute in one direction
- Difficult to compute in the other

### Examples:

### Factoring:

pq = N EASY find p, q giv en N DIFFICULT

### Discrete Log:

 $a^b \mod c = N$  EASY find b given a, c, N DIFFICULT

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### Example

Example with an 18 digit number

A = 289407349786637777

 $\mathsf{A}^2 = 83756614 \textcolor{red}{\mathbf{110525308948445338}} 203501729$ 

Middle square, B = 110525308948445338

Giv en A, it is easy to compute B

Giv en B, it is difficult to compute A

"Difficult" = no known short-cuts; requires an exhaustive search

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### Message Integrity: Digital Signatures

### Validate:

- 1. The creator (signer) of the content
- 2. The content has not been modified since it was signed

The content itself does not have to be encry pted

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## Encrypting a message with a private key is the same as signing it! Trusted directory of public keys Alice Encrypt message with Alice's private key Decrypt message with Bob's public key

### But...

- · Not quite what we want
- We don't want to permute or hide the content
- We just want Bob to verify that the content came from Alice
- Moreov er...
- Public key cryptography is much slower than symmetric encryption
- What if Alice sent Bob a multi-GB movie?

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### Hash functions

- Cry ptographic hash function (also known as a digest)
- Input: arbitrary data
- Output: fixed-length bit string
- Properties
  - One-way function
  - Given H=hash(M), it should be difficult to compute M, given H
- Collision resistant
- Given H=hash(M), it should be difficult to find M', such that H=hash(M')
- For a hash of length L, a perfect hash would take 2 (L/2) attempts
- Efficient
- Computing a hash function should be computationally efficient

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### Popular hash functions

- SHA-2
- Designed by the NSA; published by NIST
- SHA-224, SHA-256, SHA-384, SHA-512
- e.g., Linux passwords used MD5 and now SHA512
- SHA-3
- NIST standard as of 2015
- MD:
  - 128 bits (not often used now since weaknesses were found)
- · Hash functions deriverd from ciphers:
- Blowfish (used for password hashing in OpenBSD)
- 3DES used for old Linux password hashes

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### Digital signatures using hash functions

- · You:
- Create a hash of the message
- Encrypt the hash with your private key & send it with the message
- · Recipient:
- Decrypts the encrypted hash using your public key
- Computes the hash of the received message
- Compares the decrypted hash with the message hash
- If they're the same then the message has not been modified

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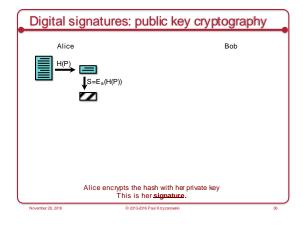
### Message Authentication Codes vs. Signatures

- Message Authentication Code (MAC)
- Hash of message encrypted with a symmetric key.
   An intruder will not be able to replace the hash value
- Digital Signature
- Hash of message encrypted with the owner's private key
- Alice encrypts the hash with her private key
- Bob validates it by decrypting it with her public key & comparing with hash(M)
- Provides non-repudiation: recipient cannot change the encrypted hash

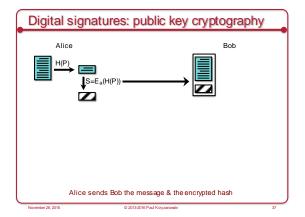
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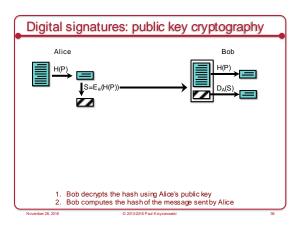
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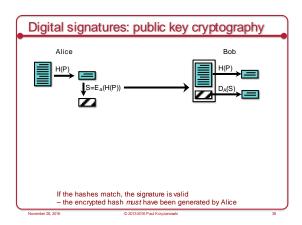
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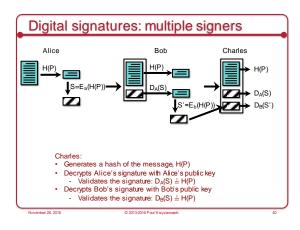


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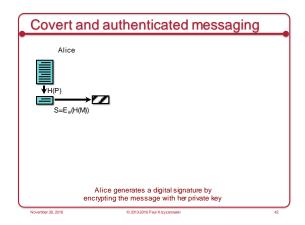












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