

# Computer Security

## 08. Cryptography – Part II

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## Block ciphers

- Block ciphers encrypt a **block** of plaintext at a time and produce ciphertext
- DES & AES are two popular block ciphers
  - DES: 64 bit blocks
  - AES: 128 bit blocks
- Block ciphers are usually **iterative ciphers**
  - The encryption process is an iteration through several **round** operations

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## Block cipher rounds

Each round consists of substitutions & permutations

**Substitution = S-box**

- Table lookup
- Converts a small block of input to a block of output
- Changing one bit of input should change approximately 1/2 of output bits

**Permutation**

- Scrambles the bits in a prescribed order

**Key application per round**

- Subkey per round derived from the key
- Can drive behavior of s-boxes
- May be XORed with the output of each round

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## Feistel cipher

- DES is a type of **Feistel cipher**, which is a form of a **block cipher**
- Plaintext block is split in two
  - Round function applied to one half of the block
  - Output of the round function is XORed with other half of the block
  - Halves are swapped
- AES is not a Feistel cipher

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## AES (Advanced Encryption Standard)

- Block cipher: 128-bit blocks
  - DES used 64-bit blocks
- Successor to DES as a standard encryption algorithm
  - DES: 56-bit key
  - AES: 128, 192, or 256 bit keys

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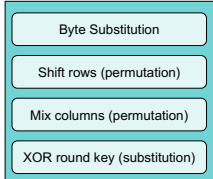
## AES (Advanced Encryption Standard)

- Iterative cipher, just like most other block ciphers
  - Each round is a set of substitutions & permutations
- Variable number of rounds
  - DES always used 16 rounds
  - AES:
    - 10 rounds: 128-bit key
    - 12 rounds: 192-bit key
    - 14 rounds: 256-bit key
  - A **subkey** ("round key") derived from the key is computed for each round
    - DES did this too

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### Each AES Round

- **Step 1: Byte Substitution (s-boxes)**
  - Substitute 16 input bytes by looking each one up in a table (S-box)
  - Result is a 4x4 matrix
- **Step 2: Shift rows**
  - Each row is shifted to the left (wrapping around to the right)
  - 1<sup>st</sup> row not shifted; 2<sup>nd</sup> row shifted 1 position to the left; 3<sup>rd</sup> row shifted 2 positions; 4<sup>th</sup> row shifted three positions
- **Step 3: Mix columns**
  - 4 bytes in each column are transformed
  - This creates a new 4x4 matrix
- **Step 4: XOR round key**
  - XOR the 128 bits of the round key with the 16 bytes of the matrix in step 3



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### AES Decryption

Same rounds  
... but in reverse order

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### DES Disadvantages

- DES has been shown to have some weaknesses
  - Key can be recovered using  $2^{47}$  chosen plaintexts or  $2^{43}$  known plaintexts
  - *Note that this is not a practical amount of data to get for a real attack*
- Short block size (8 bytes =  $2^8 = 64$  bits)
- **The real weakness of DES is its 56-bit key**
  - Exhaustive search requires  $2^{55}$  iterations on average
- 3DES solves the key size problem: we can have keys up to 168 bits.
  - Differential & linear cryptanalysis is not effective here: the three layers of encryption use 48 rounds instead of 16 making it infeasible to reconstruct s-box activity.
- DES is relatively slow
  - It was designed with hardware encryption in mind: 3DES is 3x slower than DES
  - *Still much faster than RSA public key cryptosystems!*

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### AES Advantages

- **Larger block size:** 128 bits vs 64 bits
- **Larger & varying key sizes:** 128, 192, and 256 bits
  - 128 bits is complex enough to prevent brute-force searches
- **No significant academic attacks beyond brute force search**
  - Resistant against linear cryptanalysis thanks to bigger S-boxes
    - S-box = lookup table that adds non-linearity to a set of bits via transposition & flipping
  - DES: 6-bit inputs & 4-bit outputs
  - AES: 8-bit inputs & 8-bit outputs
- **Typically 5-10x faster in software than 3DES**

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### Attacks against AES

- Attacks have been found
  - **This does *not* mean that AES is insecure!**
- Because of the attacks:
  - AES-128 has computational complexity of  $2^{126.1}$  (~126 bits)
  - AES-192 has computational complexity of  $2^{189.7}$  (~189 bits)
  - AES-256 has computational complexity of  $2^{254.9}$  (~254 bits)
- The security of AES can be increased by increasing the number of rounds in the algorithm
- However, AES-128 still has a sufficient safety margin to make exhaustive search attacks impractical

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### Cryptographic attacks

- Chosen plaintext
  - Attacker can create plaintext and see the corresponding ciphertext
- Known plaintext
  - Attacker has access to both plaintext & ciphertext but doesn't get to choose the text
- Ciphertext-only
  - The attacker only sees ciphertext
  - Popular in movies but rarely practical in real life

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### Differential Cryptanalysis

*Examine how changes in input affect changes in output*

- Discover where a cipher exhibits non-random behavior
  - These properties can be used to extract the secret key
  - Applied to block ciphers, stream ciphers, and hash functions (functions that flip & move bits vs. mathematical operations)
- Chosen plaintext attack is normally used
  - Attacker must be able to choose the plaintext and see the corresponding cipher text

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### Differential Cryptanalysis

- Provide plaintext with known differences
  - See how those differences appear in the ciphertext
- The properties depend on the **key** and the **s-boxes** in the algorithm
- Do this with lots and lots of known *plaintext-ciphertext* sets
- Statistical differences, if found, may allow a key to be recovered faster than with a brute-force search
  - You may deduce that certain keys are not worth trying

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### Linear Cryptanalysis

*Create a predictive approximation of inputs to outputs*

- Instead of looking for differences, linear cryptanalysis attempts to come up with a **linear formula** (e.g., a bunch of xor operations) that connects certain input bits, output bits, and key bits with a probability higher than random
  - Goal is to approximate the behavior of s-boxes
- It will *not* recreate the working of the cipher
  - You just hope to find non-random behavior that gives you insight on what bits of the key might matter
- Works better than differential cryptanalysis for known plaintext
  - Differential cryptanalysis works best with chosen plaintext
- Linear & differential cryptanalysis will **rarely recover a key** but may be able to reduce the number of keys that need to be searched.

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### Not a good idea to use block ciphers directly

- Streams of data are broken into *k*-byte blocks
  - Each block encrypted separately
  - This is called **Electronic Codebook (ECB)**
- Problems
  - Same plaintext results in identical encrypted blocks
    - Enemy can build up a code book of plaintext/ciphertext matches
  - Attacker can add/delete/replace blocks

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### Cipher Block Chaining (CBC) mode

- Random **initialization vector (IV)** = bunch of *k* random bits
  - Non-secret: both parties need to know this
- Exclusive-or with first plaintext block – then encrypt the block
- Take exclusive-or of the result with the next plaintext block

$$c_i = E_K(m) \oplus c_{i-1}$$

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### CBC Observations

- Identical blocks of plaintext do not produce the same ciphertext
- Each block is a function of all previous blocks
- But an attacker can still cause data corruption

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### Block encryption: Counter (CTR) mode

- Random starting **counter** = bunch of  $k$  random bits, just like IV
  - Any function producing a non-repeating sequence (an incrementing number is a common function)
- **Encrypt the counter with the key**
- Exclusive-or result with plaintext block

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### Popular symmetric algorithms

- AES (Advanced Encryption Standard)
  - FIPS standard since 2002
  - 128, 192, or 256-bit keys; operates on 128-bit blocks
- DES, 3DES
  - FIPS standard since 1976
  - 56-bit key; operates on 64-bit (8-byte) blocks
  - Triple DES recommended since 1999 (112 or 168 bits)
- Blowfish
  - Key length from 23-448 bits; 64-bit blocks
- IDEA
  - 128-bit keys; operates on 64-bit blocks
  - More secure than DES but faster algorithms are available

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### Communicating with symmetric cryptography

- Both parties must agree on a secret key,  $K$
- Message is encrypted, sent, decrypted at other side

- **Key distribution must be secret**
  - otherwise messages can be decrypted
  - users can be impersonated

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### Key Distribution

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### Key explosion

Each pair of users needs a separate key for secure communication

100 users: 4,950 keys  
1000 users: 399,500 keys

$n$  users:  $\frac{n(n-1)}{2}$  keys

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### Key distribution

Secure key distribution is the biggest problem with symmetric cryptography

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### Public-key algorithm

- Two related keys.
 
$$\begin{matrix} C = E_{K_1}(P) & P = D_{K_2}(C) \\ C' = E_{K_2}(P) & P = D_{K_1}(C') \end{matrix}$$
 $K_1$  is a **public** key  
 $K_2$  is a **private** key
- Examples:
  - RSA, Elliptic curve algorithms, DSS (digital signature standard)
- Key length
  - Unlike symmetric cryptography, not every number is a valid key
  - 3072-bit RSA = 256-bit elliptic curve = 128-bit symmetric cipher
  - 15360-bit RSA = 521-bit elliptic curve = 256-bit symmetric cipher

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### RSA Public Key Cryptography

- Ron Rivest, Adi Shamir, Leonard Adleman created a true public key encryption algorithm in 1977
- Each user generates two keys:
  - Private key (kept secret)
  - Public key (can be shared with anyone)
- Difficulty of algorithm based on the difficulty of factoring large numbers
  - keys are functions of a pair of large (~300 digits) prime numbers

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### RSA algorithm

How to generate keys

- choose two random large prime numbers  $p, q$
- Compute the product  $n = pq$
- randomly choose the encryption key,  $e$ , such that:  $e$  and  $(p - 1)(q - 1)$  are relatively prime
- Compute a decryption key,  $d$  such that:
 
$$ed = 1 \pmod{(p - 1)(q - 1)}$$

$$d = e^{-1} \pmod{(p - 1)(q - 1)}$$
- discard  $p, q$

The security of the algorithm rests on our understanding that factoring  $n$  is extremely difficult

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### RSA Encryption

- What you need:
  - Key pair:  $e, d$
  - Agreed-upon modulus  $n$
- Encrypt:
  - divide data into numerical blocks  $< n$
  - encrypt each block:
 
$$c = m^e \pmod n$$
- Decrypt:
 
$$m = c^d \pmod n$$

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### Communication with public key algorithms

Different keys for encrypting and decrypting

- No need to worry about key distribution

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### Communication with public key algorithms

The diagram illustrates the flow of keys and messages between Alice and Bob:

- Key Distribution:** Alice sends her public key ( $K_A$ ) to Bob, and Bob sends his public key ( $K_B$ ) to Alice.
- Encryption:** Alice encrypts a message ( $P$ ) using Bob's public key ( $E_B(P)$ ). Bob encrypts a message ( $P$ ) using Alice's public key ( $E_A(P)$ ).
- Decryption:** Bob decrypts the message received from Alice using his private key ( $D_B(C)$ ). Alice decrypts the message received from Bob using her private key ( $D_A(C)$ ).

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### RSA isn't good for large-scale encryption

Calculations are very expensive (& key generation is slow)  
Common speeds:

Algorithm	Bytes/sec
AES-128-ECB	148,000,000
AES-128-CBC	153,000,000
AES-256-ECB	114,240,000
RSA-2048 encrypt	3,800,000
RSA-2048 decrypt	96,000

- AES ~1500x faster to decrypt; 40x faster to encrypt
- RSA is also subject to mathematical attacks
  - Certain keys (numbers) may expose weaknesses
- If anyone learns your private key, they can read all your messages**

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### Diffie-Hellman Key Exchange

#### Key distribution algorithm

- Allows two parties to exchange keys securely
- Not public key encryption
- Based on difficulty of computing discrete logarithms in a finite field compared with ease of calculating exponentiation

Allows us to negotiate a secret **common key** without fear of eavesdroppers

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### Diffie-Hellman Key Exchange

- All arithmetic performed in a field of integers modulo some large number
- Both parties agree on
  - a **large prime number  $p$**
  - and a number  $\alpha < p$
- Each party generates a public/private key pair

Private key for user  $i$ :  $X_i$

Public key for user  $i$ :  $Y_i = \alpha^{X_i} \text{ mod } p$

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### Diffie-Hellman exponential key exchange

- Alice has secret key  $X_A$
- Alice sends Bob public key  $Y_A$
- Alice computes
- Bob has secret key  $X_B$
- Bob sends Alice public key  $Y_B$

$$K = Y_B^{X_A} \text{ mod } p$$

**$K = (\text{Bob's public key}) (\text{Alice's private key}) \text{ mod } p$**

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### Diffie-Hellman exponential key exchange

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- Bob computes

$$K = Y_B^{X_A} \text{ mod } p$$

$$K = Y_A^{X_B} \text{ mod } p$$

**$K' = (\text{Alice's public key}) (\text{Bob's private key}) \text{ mod } p$**

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### Diffie-Hellman exponential key exchange

- Alice has secret key  $X_A$
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- Alice computes
- Bob has secret key  $X_B$
- Bob sends Alice public key  $Y_B$
- Bob computes

$$K = Y_B^{X_A} \text{ mod } p$$

$$K = Y_A^{X_B} \text{ mod } p$$

expanding:

$$K = Y_B^{X_A} \text{ mod } p = (\alpha^{X_B} \text{ mod } p)^{X_A} \text{ mod } p = \alpha^{X_B X_A} \text{ mod } p$$

$$K = Y_A^{X_B} \text{ mod } p = (\alpha^{X_A} \text{ mod } p)^{X_B} \text{ mod } p = \alpha^{X_A X_B} \text{ mod } p$$

**$K = K'$**

**$K$  is a common key, known only to Bob and Alice**

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### Hybrid Cryptosystems

- **Session key**: randomly-generated key for one communication session
- Use a **public key algorithm** to send the session key
- Use a **symmetric algorithm** to encrypt data with the session key

Public key algorithms are almost never used to encrypt messages

- Vulnerable to chosen plaintext attacks
- MUCH slower; RSA-2048 approximately 40x slower to encrypt and 1,500x slower to decrypt than AES-256

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### Communication with a hybrid cryptosystem

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### Communication with a hybrid cryptosystem

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### Communication with a hybrid cryptosystem

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### Forward Secrecy

Suppose an attacker steals Bob's private key

- Future messages can be compromised
- But past messages that used the key can also be decrypted

Pick a session key  
Encrypt it with the Bob's public key

→

Bob decrypts the session key

Security rests entirely on the secrecy of Bob's private key

If Bob's private key is compromised, all recorded past traffic can be decrypted

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### Forward Secrecy

- **Forward secrecy**
  - **Compromise of long term keys does not compromise past session keys**
  - There is no one secret to steal that will compromise multiple messages
- **Diffie-Hellman**
  - Use common key as the encryption/decryption key
    - Or as a key to encrypt a session key
  - Not recoverable as long as long as private keys are thrown away after each session
  - Unlike RSA keys, Diffie Hellman makes key generation simple
- **Keys must be ephemeral**
  - Client & server will generate new Diffie-Hellman parameters for each session – all will be thrown away after the session

Diffie-Hellman is preferred over RSA for key exchange to achieve forward secrecy – generating Diffie-Hellman keys is a rapid, low-overhead process

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### Cryptographic systems: summary

- **Symmetric ciphers**
  - Based on “SP networks” = substitution & permutation sequences
- **Asymmetric ciphers** – public key cryptosystems
  - Based on **trapdoor** functions
  - Easy to compute in one direction; difficult to compute in the other direction without special information (the trapdoor)
- **Hybrid cryptosystem**
  - Pick a random session key
  - Use a public key algorithm to send
  - Use a symmetric key algorithm to encrypt traffic back & forth
- **Key exchange algorithms** (more to come later)
  - Diffie Hellman
  - Public key

*Enables secure communication without knowledge of a shared secret*

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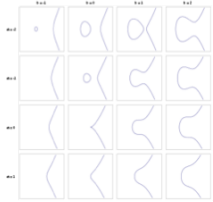
### RSA cryptography in the future

- Based on the difficulty of factoring products of two large primes
- Factoring algorithms get more efficient as numbers get larger
  - As the ability to decrypt numbers increases, the key size must therefore grow even faster
  - This is not sustainable (especially for embedded devices)

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### Elliptic Curve Cryptography

- Alternate approach: elliptic curves

$$y^2 = x^3 + ax + b$$


Catalog of elliptic curves  
[https://en.wikipedia.org/wiki/Elliptic\\_curve](https://en.wikipedia.org/wiki/Elliptic_curve)

- Using discrete numbers, pick
  - A prime number as a maximum (modulus)
  - A curve equation
  - A public base point on the curve
  - A random private key
  - Public key is derived from the private key, the base point, and the curve
- To compute the private key from the public,
  - We need an elliptic curve discrete logarithm function
  - This is difficult and is the basis for ECC's security

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### ECC vs. RSA

- **RSA is still the most widely used public key cryptosystem**
  - Mostly due to inertia & widespread implementations
  - Simpler implementation & faster decryption
- **ECC offers higher security with fewer bits than RSA**
  - ECC is also faster (for key generation & encryption) and uses less memory
  - NIST defines 15 standard curves for ECC
    - Many implementations support only a couple (P-256, P-384)
- **For long-term security**

The European Union Agency for Network and Information Security (ENISA) and the National Institute for Science & Technology (NIST) recommend:

  - AES: 256 bit keys
  - RSA: 15,360 bit keys
  - ECC: 512 bit keys

<https://www.keylength.com/en/4/>  
<http://https://www.enisa.europa.eu/publications/algorithms-key-size-and-parameters-report-2014>

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### Quantum Computers

- Once (if) real quantum computers can be built, they can
  - Crack a symmetric cipher in time proportional to the square root of the key space size:  $2^{n/2}$ 
    - Use 256-bit AES to be safe
  - Factor efficiently
    - RSA and many elliptic curve algorithms will not be secure anymore
- NSA called for a migration to “post-quantum cryptographic algorithms” – but no agreement yet on what they are

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### The End

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